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THE K-RANK NUMERICAL RADII

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ABSTRACT. The k-rank numerical range $\Lambda_k(A)$ is expressed via an intersection of any countable family of numerical ranges $\{F(M_{\nu}^*AM_{\nu})\}_{\nu \in \mathbb{N}}$ with respect to $n \times (n - k + 1)$ isometries M_{ν} . This implication for $\Lambda_k(A)$ provides further elaboration of the k-rank numerical radii of A.

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