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## ACTIONS OF ARITHMETIC FUNCTIONS ON MATRICES AND CORRESPONDING REPRESENTATIONS

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Dedicated to Professor Tsuyoshi Ando

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ABSTRACT. In this paper, we study a class of representations of arithmetic functions, and corresponding operator-theoretic and free probabilistic properties. We associate given arithmetic functions f to certain matrices  $\alpha_n(f)$ .

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