

Superordination Properties for Certain Analytic Functions ¹

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Abstract

The purpose of the present paper is to derive superordination result for functions in the class $M_{\mu}^{l,m}(\alpha, \lambda, b)$ of normalized analytic functions in the open unit disk U . A number of interesting applications of the superordination result are also considered.

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