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## Correction to \Open books and con gurations of symplectic surfaces"

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**Abstract** We correct the main theorem in \Open books and con gurations of symplectic surfaces" [1] and its proof. As originally stated, the theorem gave conditions on a con guration of symplectic surfaces in a symplectic 4-manifold under which we could construct a model neighborhood with concave boundary and describe explicitly the open book supporting the contact structure on the boundary. The statement should have included constraints on the areas of the surfaces.

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In the paper being corrected [1], we considered symplectic con guration graphs where each vertex was decorated with a triple  $(g_i; m_i; a_i)$ ,  $g_i$  being the genus of a surface,  $m_i$  its self-intersection, and  $a_i$  its symplectic area. Theorem 1.1 in [1] is false as stated. However we have the following:

**Correction 1** The conclusions of theorem 1.1 (parts A and B) are true if we add the hypothesis that there exists a constant > 0 such that, for each *i*,  $a_i = (m_i + d_i)$ .

An easy counterexample to the theorem as originally stated is given by two surfaces  $_1$  and  $_2$ , with  $_1$   $_1 = _2$   $_2 = 1$  and  $_1$   $_2 = 1$ . If  $_1 ! = a_1 \notin$  $_2 ! = a_2$ , then  $[!] \notin 0$  when restricted to the boundary of a neighborhood of  $_1 [_2$ , because [!] is nonzero when evaluated on the class  $[_1] - [_2]$ , which lives on the boundary. In general, this problem occurs when the intersection matrix for the con guration of surfaces has determinant equal to zero.

The error is on line 4 of page 583 in [1], in the calculation of  $-_{H}$ . The correct statement is:

$$_{H}^{-} = kc_{i}(d + d) - _{H}^{+}$$

Thus, to arrange that this agree with the contact pair we already have on a neighborhood of K @X, we are forced to choose  $c_i = 1$ , as opposed to

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 $c_i = a_i = (2 \quad K(m_i + d_i))$ , which was the choice made on page 582 line 22. With  $c_i = 1$ , we get that the area of i is 2  $(m_i + d_i)k$ . After the construction we can rescale by a constant to get the area to be  $(m_i + d_i)$ .

Note that, if the conguration  $_1 [ ::: [ _n is contained in a closed symplectic 4-manifold (X; !), then the area condition added in this correction is equivalent to the condition that [!] is Poincare dual to some multiple of <math>[ _1]+:::+[ _n]+$ , where  $_2 H_2(X;\mathbb{Z})$  is a class with  $_i = 0$  for i = 1;:::;n. This is because  $m_i + d_i = _1 _i + :::+ _n _i$ .

Here we emphasize that this correction does not a ect the applications in section 2 of [1], or forthcoming applications in [2].

## References

- D T Gay Open books and con gurations of symplectic surfaces, Alg. Geom. Top. 3 (2003), 569{586
- [2] **D T Gay and R Kirby** *Constructing symplectic forms on 4-manifolds which vanish on circles*, to appear

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